

Spring 2002 – Entrance Examination: Condensed Matter

Multiple choice quizzes

1. The resistivity of a solid is generally a function of temperature. Which of the following statements is correct:
 - (a) Resistivity increases with temperature in both insulators and metals
 - (b) Resistivity increases with temperature in insulators, and decreases in metals
 - (c) Resistivity decreases with temperature in insulators, and increases in metals
 - (d) Resistivity increases in metals, but is infinite in insulators.

2. The external appearance of a material is related with the nature of its energy spectrum. Thus metals are reflecting and shining because they have a lot of low-energy electronic excitations, and insulators are transparent because they have none. What is the appearance of a semiconductor like silicon, and why?
 - (a) it is reflecting and shining, because it has a small gap
 - (b) it is transparent, because it has a large gap
 - (c) it is reflecting and shining, only when heavily doped
 - (d) it is transparent because it has a gap, even if small

3. Sodium and chlorine form a ionic salt NaCl because:
 - (a) The energy obtained ionizing Cl is higher than the energy required to ionize Na. In addition, further electrostatic energy is gained in the solid.
 - (b) Energy is required to form both Na^+ and Cl^- , but the electrostatic energy gained in the solid compensates the energy cost of ions formation.
 - (c) The energy obtained ionizing Na is lower than the energy required to ionize Cl, but the electrostatic energy gained in the solid compensates the energy cost of Cl^- formation.
 - (d) The energy obtained ionizing Cl is lower than the energy required to ionize Na, but the electrostatic energy gained in the solid compensates the energy cost of Na^+ formation.

4. The quantum numbers of a multielectron atom can be labeled with the spectroscopic symbol $^{2S+1}L_J$, where S is the total spin angular momentum, L is the total orbital angular momentum and J is the total angular momentum. Only one of the following combinations exists, which one?

- (a) 1S_1
 - (b) $^2P_{1/2}$
 - (c) $^{3/2}P_{1/2}$
 - (d) 3F_1
5. Above the Curie temperature a ferromagnetic metal (Fe, Co, Ni) behaves as:
- (a) A diamagnetic material. Magnetic dipoles are completely disappeared and the magnetic susceptibility is small and negative.
 - (b) A paramagnetic material. Magnetic dipoles are still present but they are no more ordered in domains. The magnetic susceptibility is small, positive and temperature dependent.
 - (c) A paramagnetic metal. Only the Pauli paramagnetism is present. The magnetic susceptibility is small, positive and temperature independent.
 - (d) None of the above.
6. Consider a gas of hydrogen atoms at very low density. According to the principles of statistical mechanics the probability of finding an atom in the ground state is given by $P_{1s} = e^{-E_{1s}/k_B T} / Z(T)$ where $Z(T)$ is the partition function. However, $\sum_{n=1}^{\infty} n^2 e^{-E_{1s}/(k_B T n^2)}$ is clearly infinite at any non-zero temperature T . Accordingly $P_{1s} = 0$. How do you explain this apparent paradox ?
- (a) The above sum enters the classical partition function and is invalid for quantum systems.
 - (b) There is no paradox. The probability of finding an hydrogen atom in the ground state is indeed negligible.
 - (c) Inclusion of the continuum states in the partition function fixes the problem.
 - (d) The effectively finite volume per atom provides a natural cut-off to the sum over the excited states.